

Interpolation of images

FIELD OF THE INVENTION

The invention relates to a method of interpolating pixel values of pixels of an image. The invention further relates to a warped distance interpolator, and to a display apparatus comprising such a warped distance interpolator.

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BACKGROUND OF THE INVENTION

The warped distance concept (WaDi) is known from the publication "Warped distance for space-variant linear image interpolation", IEEE Transactions on Image processing, vol. 8 no. 5, May 1999 by G. Ramponi. The Warped Distance concept for linear
10 interpolators adapts a linear interpolator to the local pixel configuration of natural (non graphic) images. Particularly, the aim was to prevent edges from being blurred by the interpolation process.

The WaDi concept performs a one dimensional interpolation. In the horizontal direction, an interpolated sample could be a linear combination of the two neighboring
15 horizontal samples sandwiching the sample to be interpolated. The linear combination depends on the fractional position (or phase) of the sample to be interpolated with respect to the two neighboring horizontal samples. The interpolation at a luminance edge is adapted by locally warping the phase, such that the sample to be interpolated is virtually moved toward the right or left input sample. This warping is stronger in presence of luminance edges and
20 less on smooth parts. In order to determine the amount of warping, four pixels around the one that has to be interpolated are analyzed, and an asymmetry value is computed such that the sample to be interpolated is moved towards the flat area it belongs to.

An interpolation of a 2D image is obtained by first performing the WaDi
algorithm on the input samples in the horizontal direction to obtain interpolated horizontal
25 samples and then in the vertical direction on the interpolated horizontal samples. It is a disadvantage that a relatively complex algorithm is required.

SUMMARY OF THE INVENTION

It is an object of the invention to perform a WaDi interpolation on a two-dimensional image which provides a higher performance algorithm.

5 A first aspect of the invention provides a method of interpolating sample values of samples of an image as claimed in claim 1. A second aspect of the invention provides a warped distance interpolator as claimed in claim 7. A third aspect of the invention provides a display apparatus as claimed in claim 8. Advantageous embodiments in accordance with the invention are defined in the dependent claims.

10 The method of interpolating sample values of samples of an image determines a direction of a local gradient for a particular one of the samples from sample values neighboring the particular one of the samples. This local gradient indicates the direction of change of the values of the samples at the position of the particular sample. For example if the image comprises a white left area and a black right area and the particular sample is near to a vertical border between the white and the black area, the gradient will direct in the
15 horizontal direction towards the white area. Usually, the local gradient is determined for each output sample of the image.

Then, a warping factor for a warped distance interpolator WaDi is determined using interpolator input values arranged in the gradient direction of the particular sample. Thus, the interpolator input values for the well known WaDi interpolator are selected on a
20 line which extends through the particular sample in the direction of the local gradient.

Because usually, these interpolator input values do not coincide with the input samples, the interpolator input values have to be interpolated from input sample values neighboring the interpolator input values.

25 The determination of the warping factor in the direction of the local gradient has the advantage that the WaDi interpolation can be performed in one step, instead of performing the WaDi interpolation step successively in the horizontal and vertical direction.

In an embodiment in accordance with the invention as defined in claim 2, the WaDi interpolation is applied in a system in which an output image is a scaled input image. This approach is particularly interesting for scaling factors which are at least 2, which means
30 that the distance between the output samples is at most half of the distance between input samples. The distance may refer to the time elapsed between two successive samples or to the actual position on a display screen when these samples are displayed on the pixels of the display screen.

In this embodiment, the output image is first roughly interpolated from the input image to obtain raw interpolated data, for example by using a simple bilinear interpolator. The resultant low-pass version of the image makes the gradient estimation less susceptible to noise. A more complex interpolation, for example a cubic interpolation, may be used but has the drawback that a higher computational complexity results. The local gradient is determined by using the output pixels or raw interpolated data supplied by the simple interpolator.

In the embodiment in accordance with the invention as defined in claim 3, the local gradient is determined in the input map by using the input sample values. The local gradients found are mapped to output sample positions of the output samples in the output map. This mapping may be performed, for example, by using the nearest neighbor approach, or by linear interpolation. This approach does not require the raw interpolation step and thus takes less computational effort.

In the embodiment in accordance with the invention as defined in claim 4, the samples are arranged in a matrix in which the position of the samples is defined by the orthogonal x, y coordinates. Well known Sobel filters are used to estimate the direction of the local gradient.

In the embodiment in accordance with the invention as defined in claim 5, the distance between the adjacent interpolator input values used to determine the gradient is substantially equal to the distance between adjacent input samples to provide a coherent interpolation.

In the embodiment in accordance with the invention as defined in claim 6, the warping factor is projected on the x and y coordinates to control the WaDi interpolator to modify the distances (to warp the samples in the time domain or the pixels in the space domain) in the x and in the y direction in accordance with the projected warping factors. Thus, instead of performing the standard WaDi algorithm two times, first in the x direction to obtain intermediate results, and then in the y direction using the intermediate results, the components of the single warping factor are used to directly obtain the interpolated output samples from the input samples.

These and other aspects of the invention are apparent from and will be elucidated with reference to the embodiments described hereinafter.

BRIEF DESCRIPTION OF THE DRAWINGS

In the drawings:

Fig. 1 shows a known two step interpolation approach,

Fig. 2 shows a waveform for elucidating the known Warped Distance concept,

Fig. 3 shows, for a particular output sample, the arrangement of the interpolator input values in the direction of the local gradient in accordance with an embodiment of the invention,

Fig. 4 shows a flowchart for elucidating an embodiment of the one step Warped Distance concept in accordance with the invention,

Fig. 5 shows a flowchart of part of another embodiment of the one step Warped Distance concept in accordance with the invention, and

Fig. 6 shows a block diagram of a display apparatus comprising the Warped Distance interpolator in accordance with the invention.

DETAILED DESCRIPTION OF THE PREFERRED EMBODIMENT

Fig. 1 shows a prior art two step interpolation approach.

In well known linear interpolation techniques, a two-dimensional input image Π (see Fig. 6) is represented by input samples P_i which usually are sampled equidistant such that the input samples P_i are positioned on a rectangular grid which has a x and a y direction. The input samples P_i are also referred to as input pixels P_i which is based on the fact that if the input samples P_i were displayed on a display screen DS (see Fig. 6), the rectangular grid in time would show as a rectangular grid in position on the display screen DS . The values of the input samples P_i determine the intensity of the input pixels P_i . The output samples P_o actually to be displayed on the display screen DS may have to be interpolated from the input samples P_i to obtain output pixels P_o corresponding to the pixels on the display screen DS . This is for example required if the resolution of the display screen DS is fixed, such as is the case for matrix displays and the resolution of the input image Π differs from the resolution of the display screen DS .

Fig. 1 shows the interpolation of an output sample P_o which is positioned in-between input samples P_i . The value of the i -th input sample P_i of the j -th row of samples of the input image is denoted by $f(x_i, y_j)$. The value of the output sample P_o is denoted by $f_o(x, y)$. In Fig. 1 the four input samples P_i are shown which are nearest to the output sample P_o .

First, the input image Π is interpolated in the horizontal direction x . In the row y_j , the value $f_t(x, y_j)$ of a temporary sample P_{t1} is determined using the value $f(x_i, y_j)$ of the input sample P_i in the column x_i and the value $f(x_{i+1}, y_j)$ of the input sample P_i in the column

x_{i+1} . In the same manner, in the row y_{j+1} , the value $f(x, y_{j+1})$ of a temporary sample Pt2 is determined using the value $f(x_i, y_{j+1})$ of the input sample Pi in the column x_i and the value $f(x_{i+1}, y_{j+1})$ of the input sample Pi in the column x_{i+1} . Then, the value $f_o(x, y)$ of the output pixel Po is determined using the temporary samples Pt1 and Pt2.

5 The values of the temporary samples Pt1 and Pt2 may be calculated as

$$f(x, y_k) = (1 - S_x) f(x_i, y_k) + S_x f(x_{i+1}, y_k) \quad k = j, j+1 \quad (1)$$

wherein S_x is the distance in the x-direction between x and x_i .

The value of the output sample Po may be calculated as

$$f_o(x, y) = (1 - S_y) f(x, y_j) + S_y f(x, y_{j+1}) \quad (2)$$

10 wherein S_y is the distance in the y-direction between y and y_j .

Fig. 2 shows a waveform for elucidating the known Warped Distance concept. In the same manner as elucidated with respect to Fig. 1, the Warped Distance concept (further referred to as WaDi) determines the value of the output sample Po in two steps. The difference with the linear interpolation elucidated with respect to Fig. 1 is that the distances S_x and S_y are adapted (warped) according to a local feature of the input image II to increase the perceived quality of the interpolated output image OI (see Fig. 6). Thus, the WaDi interpolates the input image II by applying first the linear interpolation algorithm in the x-direction with an adapted distance S_x to obtain temporary or intermediate interpolated samples Pt. Then, the WaDi applies the linear interpolation algorithm in the y-direction on the intermediate interpolated samples Pt with an adapted distance S_y to obtain the output sample Po.

The WaDi warps the distances S_x and S_y based on de warping factor A:

$$A = (|a_3 - a_1| - |a_4 - a_2|) / (L - 1) \quad (3)$$

25 wherein the coefficients a_1 to a_4 are input sample values $f(x_i, y_j)$ in the neighborhood of the output sample Po to be interpolated. Depending on the step performed by the WaDi, the input samples a_1 to a_4 are arranged either in the x or in the y direction. L is the number of levels available to display the samples, for example, for 8 bit luminance signals, $L = 256$.

Fig 2 shows a waveform and input samples Pi for elucidating the WaDi in the x-direction. The function $f(x)$ shows an example of a transition in the input video image II.

30 Particularly, the aim of the WaDi was to prevent edges from being blurred by the interpolation process. If the intermediate sample Pt to be interpolated is in a position u (not shown) in the output domain, the corresponding position of the output sample Po in the input domain is $x = u/z$, wherein z is the scaling factor. The input domain comprises the input pixels Pi and the output domain comprises the output pixels Po. The fractional position or

phase $Sx = x - x_0$, wherein x_0 is the left hand input sample P_i next to x . This input sample P_i at x_0 has a sample value a_2 , the input sample P_i at x_1 has the value a_3 , the input sample P_i at x_{-1} has the value a_1 and the input sample P_i at x_2 has the value a_4 which is 1 in the examples shown. If a simple tent (bilinear) kernel is applied as the base kernel of the linear interpolator of the WaDi, the output value would be:

$$f(x) = (1 - Sx)f(x_0) + Sxf(x_1) = (1 - Sx)a_2 + Sxa_3 \quad (4)$$

wherein x_1 is the right hand input sample next to x .

Generally speaking, the interpolated sample $f(x)$ is a linear combination of the neighboring samples $f(x_0)$ and $f(x_1)$, which linear combination depends on the fractional position (or phase) Sx . The interpolation at a luminance edge is adapted by locally warping the phase Sx , such that x is virtually moved toward the right or left input sample P_i . This warping is stronger in presence of luminance edges and less in smooth parts. In order to determine the amount of warping, the four samples P_i at positions x_{-1} , x_0 , x_1 and x_2 around the sample at position x that has to be interpolated are analyzed, and an asymmetry value or warping factor A is computed:

$$A = \frac{|f(x_1) - f(x_{-1})| - |f(x_2) - f(x_0)|}{L - 1} = \frac{|a_3 - a_1| - |a_4 - a_2|}{L - 1} \quad (5)$$

wherein L is the number of allowed luminance levels (256 in case of 8-bit quantization). And x_{-1} is the input sample preceding the input sample x_0 , and x_2 is the input sample succeeding the input sample x_1 . Provided the sigmoidal edge model applies, the asymmetry value A in equation (5) is 0 when the edge is perfectly symmetric, and close to 1 (or -1) when the edge is more flat in the right (left) hand side of the sample P_t .

The sample P_t to be interpolated should be moved towards the flat area it belongs to. Therefore, when the warping factor $A > 0$, the phase Sx has to be increased, while if the warping factor $A < 0$ the phase Sx has to be decreased. This is obtained by the following warping function:

$$Sx' = Sx - kASx(Sx - 1) \quad (6)$$

where k is the general amount of warping which may be controllable. The warped phase S_x' remains in the range $[0,1]$, if k is in the range $[0,1]$. It has to be noted that the two extremes $S_x=0$ and $S_x=1$ are maintained ($S_x'=0$ and $S_x'=1$, respectively), regardless the value of A and k . The warped intermediate sample is indicated as WP.

5 In the same manner as elucidated for determining the warped intermediate samples WP by performing the known WaDi in the x direction, the WaDi has to interpolate the warped intermediate samples WP in the y -direction to obtain the output sample P_o .

Changing the phase S_x is equivalent to moving the position of the sample to be interpolated P_t or P_o in the intermediate or output grid, respectively, before applying the
 10 linear filter equation of the WaDi, as if it were warped. Actually, the final position of the samples P_t or P_o is not changed, the algorithm assigns to the sample to be interpolated P_t or P_o the value obtained as if it were in the warped position. The factor k controls the amount of warping, a greater value of k increases the sharpening effect. To be sure that the phase S_x lies within the interval 0 to 1, the factor k has to be selected ≤ 1 . But, for natural images, the
 15 factor k is preferably larger than 1. Because $|A|$ is usually small, even at these larger factors k the phase S_x is still smaller than 1. If the phase S_x becomes larger than 1 it is clipped to 1, or if it becomes smaller than 0 it is clipped to 0.

In an embodiment in accordance with the invention, compared to the known WaDi, the warping function is determined only once, in the direction of a local gradient (θ) in
 20 either the input image or the output image.

Fig. 3 shows, for a particular output sample, how the interpolator input values a_1 to a_4 may be arranged in the direction of the local gradient in accordance with an embodiment of the invention. The input samples P_i are indicated by the large dots spaced over distance d in the x, y space. The output samples P_o are indicated by the intersections of
 25 the horizontal and vertical lines which form the output grid. Fig. 3 thus shows, by way of example, a scaling with a factor 2. The line TR indicates the border between a black area (at the left hand side of the border TR) and a white area. The direction of the local gradient at the position of the output pixel P is indicated by the dotted line DLG which is perpendicular to the border TR.

30 The invention is based on changing the phases S_x and S_y , not according to local 1-dimensional features in the x or the y direction, respectively, but from 2-dimensional features. Thus, the warping factor A is calculated in one step along the local gradient direction θ which may be diagonal. It is not required to determine a factor A separately in the x -direction and in the y -direction.

As discussed with respect to the known WaDi, the asymmetry value or warping factor A is still calculated by using input values a1 to a4 which are positioned in the neighborhood of the output sample P of which the value has to be determined. But, in accordance with an embodiment of the invention, these input values are neither the input samples P_i in the x-direction nor the warped temporary samples P_t in the y-direction. Now, the input values a1 to a4 are arranged in the direction of a local gradient θ . As shown in Fig. 3, the input values a1 to a4 used to determine the warping factor A are positioned on the line DLG, thus in the direction of the local gradient θ . Usually, these input values a1 to a4 will not coincide with input samples P_i and thus will have to be interpolated from the input samples P_i . Preferably, the distance d between two successive ones of the input values a1 to a4 is equal to the sampling period of the samples P_i of the input image II to keep coherence with the image interpolation stage.

This sampling period corresponds to the distance d between two successive input samples P_i in either the x or the y direction. For example, the input values a1 to a4 are obtained by a bilinear interpolation in the positions shown in Fig. 3. These positions of the input values a1 to a4 are selected along the maximum gradient direction θ , at distances $-1.5 \cdot d$, $-0.5 \cdot d$, $0.5 \cdot d$, $1.5 \cdot d$, respectively, from the (x_p, y_p) position of the output pixel P to be interpolated, wherein d is the distance between two successive input pixels P_i in the input grid. The coordinates x and y of the input values a1 to a4 are determined with the following equations:

$$\begin{aligned} x &= x_p + (i - 2.5)d \cdot \cos(\theta) \\ y &= y_p + (i - 2.5)d \cdot \sin(\theta) \end{aligned}$$

wherein i is the index of the input value a_i .

Two possible embodiments are elucidated for determining the local gradient θ . In the first embodiment, the input image II is first interpolated with a known algorithm, for example with a bilinear filter, to obtain roughly interpolated output samples. The local gradient θ is determined in the output domain from these output samples. For example, by using a Sobel filter. Possible masks of Sobel filters to obtain a value of the directional derivative along x and y directions are:

$$Sobel_x = \begin{pmatrix} 1/4 & 0 & -1/4 \\ 1/2 & 0 & -1/2 \\ 1/4 & 0 & -1/4 \end{pmatrix} \quad Sobel_y = \begin{pmatrix} -1/4 & -1/2 & -1/4 \\ 0 & 0 & 0 \\ 1/4 & 1/2 & 1/4 \end{pmatrix}$$

The direction of the gradient θ at the position x_i, y_j is then estimated as follows:

$$\theta(x_i, y_j) = \arctan((f1 * Sobel_y) / (f1 * Sobel_x)) \quad (7)$$

wherein $f1$ is the result of the rough interpolation of the input image Π , and θ is an angle which varies between $-\pi/2$ and $\pi/2$.

The gradient evaluation has been performed by using Sobel's method in the output domain. A pre-processing, for example a simple bilinear interpolator, is required to obtain raw interpolated output samples which represent a low-pass version of the input image Π and thus the gradient estimation is less noise-sensitive. The rough interpolation may be performed with more complex methods, for example, such as a bicubic interpolation, which of course has the drawback that a higher computational complexity is required but which provides better gradient values θ . Although this first embodiment provides a very good gradient estimate, it adds a considerable overhead to the total processing time.

In another embodiment, a less optimal solution to estimate the gradient θ is to apply the Sobel filters in the input domain (using the input samples P_i) and then map these gradient values to the output grid. This mapping may be performed, for example, by using the nearest neighbor approach, or by linearly interpolating the estimated gradient values θ .

If very high values of the interpolation factor are required, the pass band of Sobel filter could become too large and the gradient estimation would not work. For high interpolation factors, it is thus better to resize the image in two steps, performing the whole algorithm twice. For example, an interpolation by a factor of 8 may become an interpolation by a cascade of interpolations by a factor of 2. Alternatively, the Sobel filters may be used to process a mid-resolution version of the input image Π to obtain gradient values θ . The same gradient values θ are assigned to a group of output pixels P_o in the ultra-high resolution output grid.

Fig. 4 shows a flowchart for elucidating an embodiment of the one step Warped Distance concept in accordance with the invention.

The step 1 receives the input samples $P_i(i,j)$ and supplies local gradients $\theta(m,n)$ (also referred to as gradients). In the first embodiment as elucidated before, the step 10 interpolates the input pixels $P_i(i,j)$ to obtain estimated output samples $I'(m,n)$ which are inputted into the Sobel_x filtering step 11 and the Sobel_y filtering step 12. In the dividing step 13, the output of the Sobel_y filtering step 12 is divided by the output of the Sobel_x filtering step 11. Step 14 determines the gradient $\theta(m,n)$ by calculating the arctan of the output of the dividing step 13.

The step 2 performs the local asymmetry estimation also referred to as

the determination of the warping factor A. In step 20, the four input values a1 to a4 are selected to be determined in positions along the direction of the local gradient θ , thus on the line DLG. P(m,n) is the output sample of which the value has to be interpolated, and $\theta(P)$ is the local gradient at the position of this output sample P(m,n). In step 21, the values of the input values a1 to a4 are determined by interpolation of the input samples P_i surrounding the positions of the input values a1 to a4. Preferably, a bilinear interpolation is used. In step 22, the warping factor A is determined according to equation 5 in one step from the interpolated input values a1 to a4.

The step 3 determines the values of the output samples $P_o(i,j)$. Step 30 receives the gradients $\theta(m,n)$ and the warping factor A to compute the local warping components or distances SL_x and SL_y by warping the distances S_x and S_y in the same manner as equation 6 did for the known WaDi approach. To obtain the result, the warping vector A is projected onto the x and y direction. The following equations perform these operations:

$$SL_x = S_x + kA \cos(\theta)/4 \quad (8)$$

$$SL_y = S_y + kA \sin(\theta)/4 \quad (9)$$

As in the known WaDi approach, k is a multiplying factor that adjusts the distortion intensity, θ is the angle which defines the gradient direction. The optional factor 4 at the denominator is provided only for comparison with the known WaDi results. Note that the k factor can be varied on a sample-per-sample (or if referring to the output pixels on a pixel by pixel) basis, by means of an (external) automatic control. For example, a natural content detector can be used to estimate the probability whether the local pixel is part of a photograph. Depending on this estimate the warping effect can be tuned via the k factor to obtain the best result.

The optional clipping step 31 clips the values of the local warping distances SL_x and SL_y to keep them in a range from zero to one, including the limits. Otherwise, it may happen, especially if the multiplying factor $k > 4$, that the warping distances SL_x or SL_y are smaller than zero or greater than one which means that the output pixel P_o to be interpolated would move outside the square formed by the four nearest input pixels P_i , which will not provide a good interpolation. The clipped warping distances are denoted by SLC_x and SLC_y .

It has to be noted that based on equations 8 and 9, that if the phase $S_x=0$ and the phase $S_y=0$, and if A is not zero, the warping distances SL_x and SL_y may not be equal to

zero. Thus, output pixels $P_o(m,n)$ interpolated in points of the output grid that correspond to points in the input grid may have a value different from the corresponding input samples $P_i(i,j)$. Therefore, the adapted WaDi algorithm in accordance with the invention is an approximate interpolation algorithm.

- 5 The interpolation step 32 interpolates the input samples $P_i(i,j)$ with an interpolator which preferably uses a linear kernel. The clipped warping distances SLC_x and SLC_y determine how the output sample $P_o(m,n)$ has to be interpolated by weighting the adjacent input samples $P_i(i,j)$ in the same manner as in the known WaDi.

- 10 The warped position x',y' in which the value $f(x',y')$ of the output sample or pixel $P_o(x,y)$ has to be evaluated is influenced by three factors:

the coordinates x,y of the output pixel P_o we are interpolating,
the direction θ of the local gradient which constrains the position of the input values a_i used to calculate the warping factor A , and
the value of the warping strength parameter k .

- 15 Fig. 5 shows a flowchart of part of another embodiment of the one step Warped Distance concept in accordance with the invention. Fig. 5 shows the steps required in the step 1 which determines the direction of the local gradient $\theta(m,n)$ in accordance with the second embodiment discussed before. Now, step 1 comprises the steps 15 and 16 instead of the steps 10 to 14 shown in Fig. 4. In step 15, the direction of the local gradients $\theta(i,j)$ is
20 determined in the input image II for the input samples P_i . The step 16 maps these local gradients $\theta(i,j)$ from the input domain to the output domain to obtain local gradients $\theta(m,n)$ for the output pixels P_o . The other steps of the WaDi processing of this embodiment in accordance with the invention are equal to the steps shown in Fig. 4.

- 25 Fig. 6 shows a block diagram of a display apparatus comprising the Warped Distance interpolator in accordance with the invention. An input video processor IVP processes input video IV to obtain the input image II comprising the input samples P_i . If the input video IV comprises the three RGB signals, the input video processor IVP may comprise a matrix for determining the luminance value. The scaler WI comprises the WaDi interpolator in accordance with the invention which is the known WaDi interpolator which is
30 adapted to be able to process two-dimensional input images II in one step. The scaler WI supplies the output image OI which comprises the output samples P_o . Such a scaler is usually required in display apparatuses which comprise a matrix display. Such a matrix display has a native resolution determined by the number of pixels (display elements) in each row and the number of rows. On the other hand, the input image II has a resolution which may differ from

the native resolution of the matrix display. Thus, the output samples P_o to be displayed on the pixels of the matrix display have to be interpolated from the input samples P_i . The scaler WI may receive the input video IV to be able to interpolate each of the three signals R, G and B, if present. The output video processing processes the output video OI to obtain a video drive
5 signal VDS suitable to drive the display device DP comprising the display screen DS.

To conclude, the preferred embodiment in accordance with the invention is directed to a digital processor which performs the next steps in the order given.

Interpolate 10 the input image II with a predetermined fast interpolation method to obtain a roughly interpolated output image $I'(m,n)$ comprising temporary output
10 samples P_{ot} . The temporary output samples P_{ot} are determined for the purpose of using them to calculate the local gradient direction $\theta(m,n)$ and are not meant to be displayed.

Calculate the local gradient direction $\theta(m,n)$ in this roughly interpolated output image $I'(m,n)$ with a simple algorithm such as the Sobel filters 11 and 12, the divider 13 and the arctan calculator 14, but other algorithms may also be used.

15 Determine 21 a number of interpolated input values a_i along this gradient direction $\theta(m,n)$ from the input samples $P_i(i,j)$ of the input image II in selected 20 predetermined positions located around the output pixel $P_o(m,n)$ we want to interpolate. Use these input values a_i to match the edge model of the WaDi approach by calculating 22 the warping factor A. Use this warping factor A to calculate the warping along the gradient
20 direction $\theta(m,n)$.

Project 30 the calculated warping along the gradient direction $\theta(m,n)$ on the x and y axis, and perform a clipping 31 if necessary. Apply 32 the projected x and y warping components on the values of the phases S_x and S_y (representing the offset of the output samples $P_o(m,n)$ to be interpolated with respect to the closest upper-left input pixels $P_i(i,j)$)
25 to calculate the warped position of the output sample $P_o(m,n)$. Use 32 a linear filtering technique to interpolate the output sample value $P_o(m,n)$ in the warped position accordingly. The output samples $P_o(m,n)$ are used to be displayed.

The WaDi algorithm in accordance with the invention could be used every time an interpolation processing is required of photographic images or video. The algorithm
30 performs best when scaling factors greater than 2 are required. For example, the algorithm may be used in video-wall applications, in photo-retouching software and other context. It could also be useful inside integrated circuits, such as, for example controllers of digital display systems. The algorithm could be implemented both in real time and batch processing applications.

It should be noted that the above-mentioned embodiments illustrate rather than limit the invention, and that those skilled in the art will be able to design many alternative embodiments without departing from the scope of the appended claims.

Although the WaDi processing in accordance with the invention has been
5 described for grey scale images, the same processing can be used for color images. If the WaDi processor receives RGB (Red, Green and Blue) input signals, the warped distances SLx and SLy may be calculated by using the luminance value determined from the RGB input signals. The difference is that in the last step 32, the interpolation is applied three times, on
10 each one of the RGB signals separately using the same values of the warped distances SLx and SLy or the clipped warped distances SLCx, SLCy.

In the claims, any reference signs placed between parentheses shall not be construed as limiting the claim. Use of the verb "comprise" and its conjugations does not exclude the presence of elements or steps other than those stated in a claim. The article "a" or "an" preceding an element does not exclude the presence of a plurality of such elements. The
15 invention may be implemented by means of hardware comprising several distinct elements, and by means of a suitably programmed computer. In the device claim enumerating several means, several of these means may be embodied by one and the same item of hardware. The mere fact that certain measures are recited in mutually different dependent claims does not indicate that a combination of these measures cannot be used to advantage.